Worksheet for graph theory lecture 13

Given the graph below, draw the following edge induced subgraphs (see lecture 9):

$$G[\{a, b, e\}], G[\{a, b, f, g, h\}]$$

Also, with the same graph, find subsets $S_1, S_2 \subset E[G]$ such that $G[S_1], G[S_2]$ are the blocks of G.



Problem (corrected!): Suppose that v is a cut vertex in a graph G, and let $H_1, H_2, H_3, \ldots, H_k$ be the different components in G - v. Show that if $C \subset G$ is a cycle containing v, then C can only intersect one of these components -- i.e. $C \cap H_i = \emptyset$ for all but one value of i.

Problem: Show that if e is an edge in G, then G is nonseparable if and only if G[[e]] is nonseparable.

Problem: Show that if G is nonseparable, than any two edges lie on a common cycle (use the subdivision strategy of the video).